Practice Test Answer and Alignment Document Mathematics - Grade 10

Part A

| Item Number | Answer Key | Kentucky <br> Academic <br> Standard | Mathematical Practices |
| :---: | :---: | :---: | :---: |
| 1. | D | KY.HS.N. 2 | MP. 8 |
| 2. |  | KY.HS.F.4.a | MP.4, MP. 5 |
| 3. | See rubric | KY.HS.F.7.a | MP.4, MP. 5 |
| 4. |  | KY.HS.A.25.b | MP. 6 |



## Part B

| Item Number | Answer Key | Kentucky Academic Standard | Mathematical Practices |
| :---: | :---: | :---: | :---: |
| 1. | Kim's <br> equation would be most appropriate to use to predict a population of $\square$ 14,745 people in a town with an area of 7.2 square kilometers. | KY.HS.SP.6.a | MP.2, MP. 8 |
| 2. | C, E | KY.HS.G. 6 | MP. 1 |
| 3. | See rubric | KY.HS.F.5.a | MP. 2 |
| 4. | $\mathbf{0 . 3}$ or equivalent number | KY.HS.SP.8.a | MP. 5 |
| 5. | $x=\frac{3+\sqrt{ } 189}{10}$ and $x=\frac{3-\sqrt{ } 189}{10}$ or equivalent numbers | KY.HS.A.19.a | MP. 7 |
| 6. | See rubric | KY.HS.F.3.a | MP.2, MP. 4 |
| 7. | D | KY.HS.F.3.a | MP. 2 |

## Rubrics

## Part A \#3

Rubric

| Score Point 2 | Student demonstrates a complete understanding of using the formula for an arithmetic sequence to model a situation. |
| :---: | :---: |
| Score Point 1 | Student demonstrates a partial understanding of using the formula for an arithmetic sequence to model a situation. |
| Score Point 0 | Student response is insufficient to demonstrate a grade-appropriate, relevant understanding of the task. |
| Score Points | - Score 2 points: <br> - Correct formula with a complete explanation. <br> - Score 1 point: <br> - Correct formula with a partial explanation. OR <br> - Explanation indicates a partial understanding of using the formula for an arithmetic sequence to generate terms. |
| Correct Answer | The sequence increases by 3 from one term to the next. I determined this by finding the rate of change. $\frac{23-2}{8-1}=\frac{21}{7}=3$ <br> Then I used the formula $a_{n}=a_{1}+(n-1) d$ to write an equation that could be used to find the $n$th term of the arithmetic sequence. The initial value, $a_{1}$, is 2 . The common difference, $d$, is 3 . $a_{n}=2+3(n-1)$ <br> Note: <br> - Other valid explanations are acceptable. <br> - Equivalent equations are acceptable. <br> - Variable substitution is allowed. |

## Part A \#5

## Rubric

The total item score is the sum of points awarded in the Machine-scored and Human-scored parts.

## Machine Scoring

| Machine Scoring |  |
| :---: | :---: |
| Score Point 1 | Part A <br> Student response is the correct graph of $f(x)$, with the vertex at $(-1,-3)$. |
| Score Point 0 | Student response is incorrect. |
| Human Scoring |  |
| Score Point 3 | Student scores a total of 3 points. |
| Score Point 2 | Student response is incorrect. |
| Score Point 1 | Student demonstrates a minimal understanding of comparing the properties of two functions, each represented in a different way. |
| Score Point 0 | Student response is insufficient to demonstrate a grade-appropriate, relevant understanding of the task. |
| Score Points | Part B <br> - Score 3 points: <br> - Complete explanations of how the two functions compare using their values. <br> - Score 2 points: <br> - Complete explanation of how the minima compare using their values with a partial explanation of how the widths compare. OR <br> - Complete explanation of how the widths compare using their values with a partial explanation of how the minima compare. <br> - Score 1 point: <br> - Partial explanation of how the minima compare using their values with a partial explanation of how the widths compare. OR <br> - Only one of the explanations is complete. OR <br> - Partial explanation of how the minima compare using their values with a minimal explanation of how the widths compare. OR <br> - Partial explanation of how the widths compare using their values with a minimal explanation of how the minima compare. OR <br> - Explanations of how the two functions compare with no references to their values. |
| Correct Answer | Part B <br> The minimum of $f(x)$ is $(-1,-3)$ and is located below the minimum of $g(x)$ which is $(1,2)$. <br> The width of is $f(x)$ represented by the value of 2 , and the width of $g(x)$ is represented by the value of 1 . Function $g(x)$ is wider than $f(x)$ because the lesser the value of $a$ the wider the shape of the parabola. |

## Part B \#3

## Rubric

| Score Point 4 | Student scores 4 points. |
| :---: | :---: |
| Score Point 3 | Student scores 3 or 3.5 points. |
| Score Point 2 | Student scores 2 or 2.5 points. |
| Score Point 1 | Student scores $0.5,1$, or 1.5 points. <br> OR <br> Student demonstrates a minimal understanding of identifying zeros and extreme values of the graph within the context of a quadratic function. |
| Score Point 0 | Student response is insufficient to demonstrate a grade-appropriate, relevant understanding of the task. |
| Score Points | Part A <br> - Score 2 points: <br> - Correct answers with a complete explanation or work provided. <br> - Score 1.5 points: <br> - Correct answers with a partial explanation or work provided. <br> - Score 1 point: <br> O Correct answers with no work or explanation provided. OR <br> - One correct answer with valid work or explanation provided. <br> - Score 0.5 point: <br> - Demonstrates a minimal understanding of the extreme value of the graph within the context of a quadratic function. <br> Part B <br> - Score 2 points: <br> - Correct answers with a complete explanation or work provided. <br> - Score 1.5 points: <br> - Correct answers with a partial explanation or work provided. <br> - Score 1 point: <br> - Correct answers with no work or explanation provided. OR <br> - Incomplete explanation with zeros identified without specifying the meaning of the zeros. <br> - Score 0.5 point: <br> - Demonstrates a minimal understanding of identifying zeros of the graph within the context of a quadratic function. |
| Correct Answer | Part A <br> The maximum value of $P(x)$ is the vertex located at $(3,225)$ on its graph. The point represents the price that would yield the maximum weekly profit. <br> The price of $\$ 3$ will yield a maximum weekly profit of $\$ 225$. <br> Part B <br> The prices that would make the weekly profit $\$ 0$ are $\$ 0$ and $\$ 6$ because the zeros of the function are: $\begin{aligned} & 0=-25 x^{2}+150 x \\ & 0=-25 x(x-6) \\ & 0=-25 x \text { and } 0=x-6 \\ & 0=x \text { and } 6=x \end{aligned}$ |

## Part B \#6

## Rubric

| Score Point 2 | Student demonstrates a complete understanding of calculating and interpreting the average rate of change of a function presented as a table over a specified interval. |
| :---: | :---: |
| Score Point 1 | Student demonstrates a partial understanding of calculating and interpreting the average rate of change of a function presented as a table over a specified interval. |
| Score Point 0 | Student response is insufficient to demonstrate a grade-appropriate, relevant understanding of the task. |
| Score Points | - Score 2 points: <br> - Correct value and interpretation. <br> - Score 1 point: <br> - Correct value. OR <br> - Correct interpretation. |
| Correct Answer | The average rate of change is $\frac{2}{7}$. The plant's height increases at an average rate of $\frac{2}{7}$ centimeters per day. <br> NOTE: Other reasonable interpretations of the average rate of change are acceptable. |

